

Compute the limit, if it exists. If it does not exist, write "DNE". In either case, include some steps to support your answer.

$$1.] (2 \text{ pts}) \quad \lim_{x \rightarrow -0.5} 1 - 2x^2 = 1 - 2(-0.5)^2 = 1 - 2(0.25) = 1 - 0.5 = 0.5.$$

$$2.] (2 \text{ pts}) \quad \lim_{x \rightarrow -2} \frac{4 - x^2}{x + 2} = \lim_{x \rightarrow -2} \frac{(2+x)(2-x)}{x+2} = \lim_{x \rightarrow -2} 2 - x = 2 - (-2) = 4.$$

$$3.] (2 \text{ pts}) \quad \lim_{x \rightarrow \infty} \frac{x^3 + 5}{9x - 5x^3} = \lim_{x \rightarrow \infty} \frac{x^3/x^3 + 5/x^3}{9x/x^3 - 5x^3/x^3} = \lim_{x \rightarrow \infty} \frac{1 + 5/x^3}{9/x^2 - 5} = \frac{1+0}{0-5} = -\frac{1}{5}.$$

$$4.] (2 \text{ pts}) \quad f(x) = \begin{cases} x^3 & \text{if } x < 2 \\ 8 & \text{if } x \geq 2 \end{cases}$$

$$a.) \lim_{x \rightarrow 2^-} f(x) = \lim_{x \rightarrow 2^-} x^3 = (2)^3 = 8.$$

$$b.) \lim_{x \rightarrow 2^+} f(x) = \lim_{x \rightarrow 2^+} 8 = 8.$$

$$c.) \lim_{x \rightarrow 2} f(x) = 8, \text{ since the left and right handed limits both equal } 8.$$

d.) Is $f(x)$ continuous at $x = 2$? Why or why not?

$$\text{Yes, since } \lim_{x \rightarrow 2} f(x) = f(2).$$

5.] (2 pts) Two species coexist in the same ecosystem. Species I has population $P(t)$ in t years, while Species II has population $Q(t)$, both in thousands, where P and Q are modeled by the functions

$$P(t) = \frac{30}{3+t}$$

$$Q(t) = \frac{64}{4-t}$$

for all times $t \geq 0$ for which the respective populations are not negative.

What happens to $P(t)$ as t increases? (As always, justify your answer)

(The population goes "extinct")
 $\lim_{t \rightarrow \infty} \frac{30}{3+t} = 0$ since the limit of the numerator exists (not infinite) and the limit of the denominator is ∞ .

What happens to $Q(t)$ as t increases? (Justify)

Note $t < 4$ since $Q(4)$ is undefined and for $t > 4$, $Q(t)$ is negative.

$\lim_{t \rightarrow 4^-} \frac{64}{4-t} = \infty$ since the limit of the numerator exists (not infinite) and is not zero, and the limit of the denominator is zero, and $4-t$ is positive for $t < 4$.

(The population "explodes")