

1. For each problem, I have listed two different functions that have the given derivative.

(a) • $y = 3x + 2$
• $y = 3x - 3$

(b) • $y = x^3 + 5$
• $y = x^3 - 7$

(c) • $w = 2x^4 - \frac{1}{3}x^3 + \frac{5}{2}x^2 - 10x + 11$
• $w = 2x^4 - \frac{1}{3}x^3 + \frac{5}{2}x^2 - 10x - 13$

(d) • $h = 4 \ln(t) + 17$
• $h = 4 \ln(t) - 19$

(e) • $y = 30e^x + 5x + 23$
• $y = 30e^x + 5x - 29$

(f) • $q = -50e^{-t} + 31$
• $q = -50e^{-t} - 37$

(g) • $P = \frac{1}{4}t^4 - \frac{1}{2}t^{-2} + 41$
• $P = \frac{1}{4}t^4 - \frac{1}{2}t^{-2} - 43$

(h) • $y = \ln(x + 4) + 47$
• $y = \ln(x + 4) - 53$

(i) • $z = \frac{1}{3}e^{3y} + 59$
• $z = \frac{1}{3}e^{3y} - 61$

(j) • $v = -100e^{-r} + 67$
• $v = -100e^{-r} - 71$

(k) • $s = 4e^t - 3^{-t} + 73$
• $s = 4e^t - 3^{-t} - 79$

(l) • $P = 2\sqrt{t} + 83$
• $P = 2\sqrt{t} - 89$

(m) • $P = 2 \ln(t) + 3t^{-1} + 97$
• $P = 2 \ln(t) + 3t^{-1} - 101$

(n) • $h = 15e^{2s} + \frac{1}{3}e^{3s} + 103$
• $h = 15e^{2s} + \frac{1}{3}e^{3s} - 107$

(o) • $P = 100e^{0.05t} + 109$
• $P = 100e^{0.05t} - 113$

(p) • $y = \frac{1}{2}e^{x^2} + 127$
• $y = \frac{1}{2}e^{x^2} - 131$

(q) • $y = (x^2 + 1)^4 + 137$
• $y = (x^2 + 1)^4 - 139$

(r) • $y = \frac{8}{3}(x^3 + 7)^{3/2} + 149$
• $y = \frac{8}{3}(x^3 + 7)^{3/2} - 151$

(s) • $y = 6e^{-0.25x^2} + 157$
• $y = 6e^{-0.25x^2} - 163$

2. The indefinite integral represents the most general antiderivative of the integrand and so is an entire family of functions (hence the $+C$).

$$(a) \int 3 dx = 3x + C$$

$$(b) \int 3x^2 dx = x^3 + C$$

$$(c) \int (8x^3 - x^2 + 5x - 10) dx = 2x^4 - \frac{1}{3}x^3 + \frac{5}{2}x^2 - 10x + C$$

$$(d) \int \frac{4}{t} dx = 4 \ln(t) + C$$

$$(e) \int (30e^x + 5) dx = 30e^x + 5x + C$$

$$(f) \int 50e^{-t} dt = -50e^{-t} + C$$

$$(g) \int \left(t^3 + \frac{1}{t^3}\right) dt = \frac{1}{4}t^4 - \frac{1}{2}t^{-2} + C$$

$$(h) \int \frac{1}{x+4} dx = \ln(x+4) + C$$

$$(i) \int e^{3y} dy = \frac{1}{3}e^{3y} + C$$

$$(j) \int \frac{100}{e^r} dr = -100e^{-r} + C$$

$$(k) \int (4e^t + 3e^{-t}) dt = 4e^t - 3e^{-t} + C$$

$$(l) \int \frac{1}{\sqrt{t}} dt = 2\sqrt{t} + C$$

$$(m) \int \left(\frac{2}{t} - \frac{3}{t^2} \right) dt = 2 \ln(t) + 3t^{-1} + C$$

$$(n) \int (30e^{2s} + e^{3s}) ds = 15e^{2s} + \frac{1}{3}e^{3s} + C$$

$$(o) \int 5e^{0.05t} dt = 100e^{0.05t} + C$$

$$(p) \int xe^{x^2} dx = \frac{1}{2}e^{x^2} + C$$

$$(q) \int 8x(x^2 + 1)^3 dx = (x^2 + 1)^4 + C$$

$$(r) \int 12x^2\sqrt{x^3 + 7} dx = \frac{8}{3}(x^3 + 7)^{3/2} + C$$

$$(s) \int -3xe^{-0.25x^2} dx = 6e^{-0.25x^2} + C$$