

## HOMEWORK 2

Problems assigned up to and including **Friday, 09/05**. The solutions are due on **Friday, 09/12**.

**ASSIGNED WEDNESDAY, 09/03.**

Section 1.3: 8, 12.

**Problem A:** Denote by  $\mathcal{S}$  the set of all subsets  $A \subset \mathbb{N}$  for which both  $A$  and  $\mathbb{N} \setminus A$  are **infinite** (not uncountable, as I originally – and mistakenly – wrote). Prove that  $\mathcal{S}$  is uncountable.

**Problem B:** Suppose  $A$  is an infinite set, and  $B$  is a countable set. Prove that the sets  $A$  and  $A \cup B$  are equipollent.

**Problem C (bonus):** For a set  $A$ , denote by  $A^{\mathbb{N}}$  the set of all infinite sequences of elements of  $A$ . Show that  $\mathbb{R}^{\mathbb{N}}$  (the set of all sequences of real numbers) is equipollent with  $\mathbb{R}$ . You can use the fact that  $\mathbb{R}$  is equipollent with the power set of  $\mathbb{N}$ , and identify the latter with the set of all 0 – 1 sequences.

**ASSIGNED FRIDAY, 09/05.**

Section 2.1: 1(b), 2(b).

Back to the syllabus.

Back to the main page of the course.

The solutions.