

### SOLUTION #3 (8 AM)

**Solution 1.** If  $f(x)$  gets closer and closer to a number  $L$  as  $x$  gets closer and closer to  $c$  from both sides, then  $L$  is the limit of  $f(x)$  as  $x$  approaches  $c$ . (2pts)

**Solution 2.** (1)  $\lim_{x \rightarrow 0} \frac{x(x+1)}{x^2+1} = \frac{0(0+1)}{0+1} = 0$  (3pts)

(2)  $\lim_{x \rightarrow \infty} \frac{x^4+1}{8-x^3} = \lim_{x \rightarrow \infty} \frac{\frac{1}{x^3}(x^4+1)}{\frac{1}{x^3}(8-x^3)}$  (1pt)

$$= \lim_{x \rightarrow \infty} \frac{x + \frac{1}{x^3}}{\frac{8}{x^3} - 1}$$
 (1pt)

$$= \lim_{x \rightarrow \infty} -x = -\infty$$
 (1pt)

(3)  $\lim_{x \rightarrow \infty} \frac{1-\sqrt{x}}{1+\sqrt{x}} = \lim_{x \rightarrow \infty} \frac{\frac{1}{\sqrt{x}}(1-\sqrt{x})}{\frac{1}{\sqrt{x}}(1+\sqrt{x})}$  (1pt)

$$= \lim_{x \rightarrow \infty} \frac{\frac{1}{\sqrt{x}} - 1}{\frac{1}{\sqrt{x}} + 1} = \frac{0-1}{0+1} = -1$$
 (1pt)